



GCSE

MATHEMATICS

GCSE Maths Predicted Paper 1

2026 (May): Non-Calculator

Set 1

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A/Prof (Dr) Nathan



GCSE Maths Predicted Papers 2026 (May)
Paper 1: Non-Calculator (Set 1)
Duration: 1 hour and 30 minutes

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This GCSE Maths paper 1 (Predicted Paper May 2026: Set 1) has been created based on the most common topics from previous past papers. This paper should be excellent for helping students revise for exams; however, it should not be relied upon as the sole basis for revision.

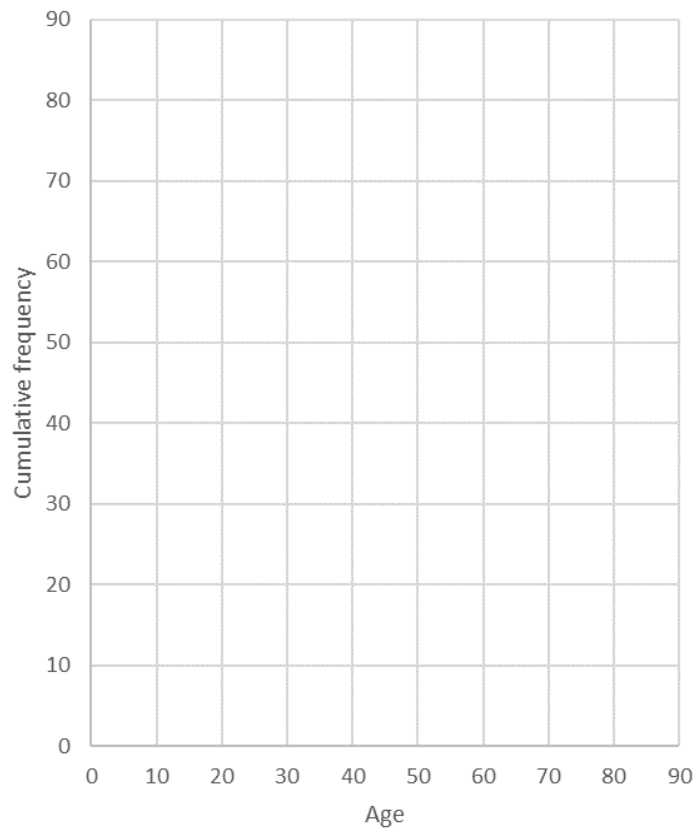
Grade Boundary: Grade 8: 71% and Grade 9: 84%

13.

The cumulative frequency table gives information about the ages of 90 people working for a company.

Age (x years)	Cumulative frequency
$20 < x \leq 30$	19
$20 < x \leq 40$	37
$20 < x \leq 50$	60
$20 < x \leq 60$	82
$20 < x \leq 70$	90

- (a) On the grid below, draw a cumulative frequency graph for this information
- (b) Use your graph to find an estimate for the Median Age, and Interquartile Range (IQR)



(3)



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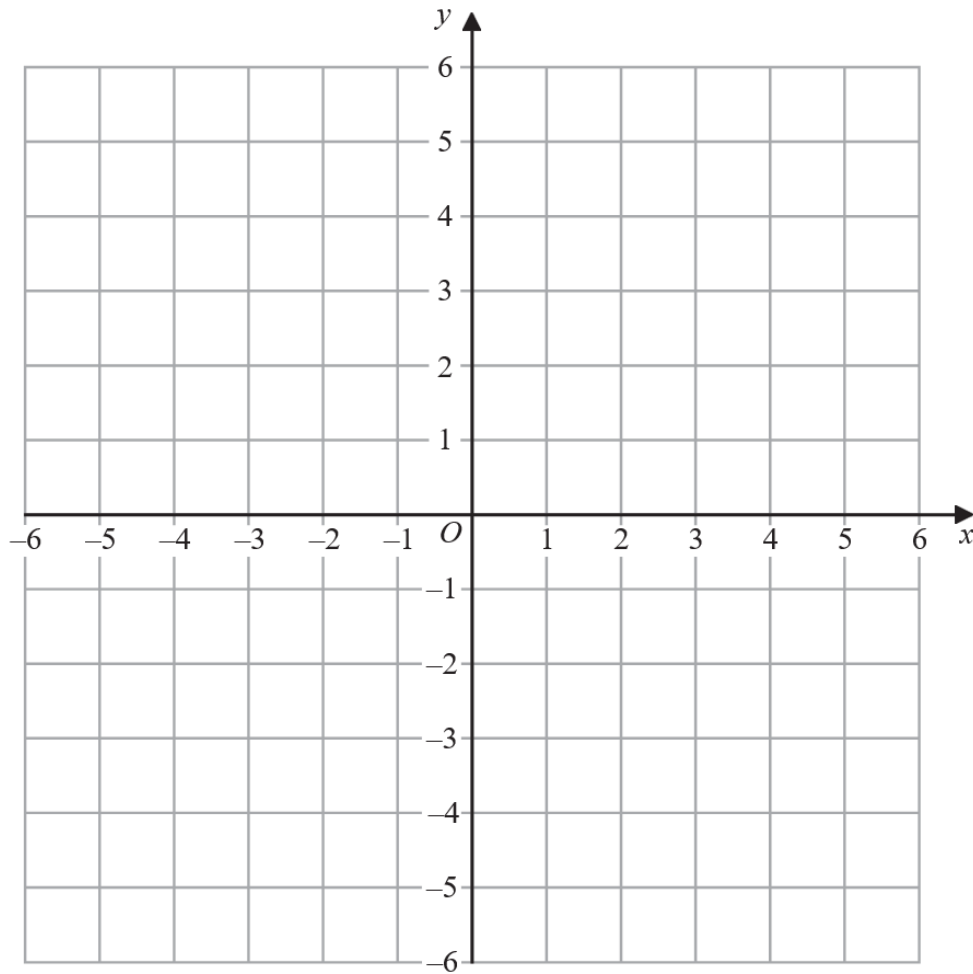
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15.

Draw the graph of $y = 2^x$ $-2 \leq x \leq 2$



(b) The graph of the function $y = ab^x$ goes through the points (1,8) and (4,64). Find a and b.

(4)



19.

Using algebra, find the value of $\frac{0.3\dot{5}}{0.5\dot{5}}$

(3)

20.

k is inversely proportional to the square of p.

$k = 1.0$ when $P = \sqrt{7}$.

Find the value of k when $p = 10$

(3)



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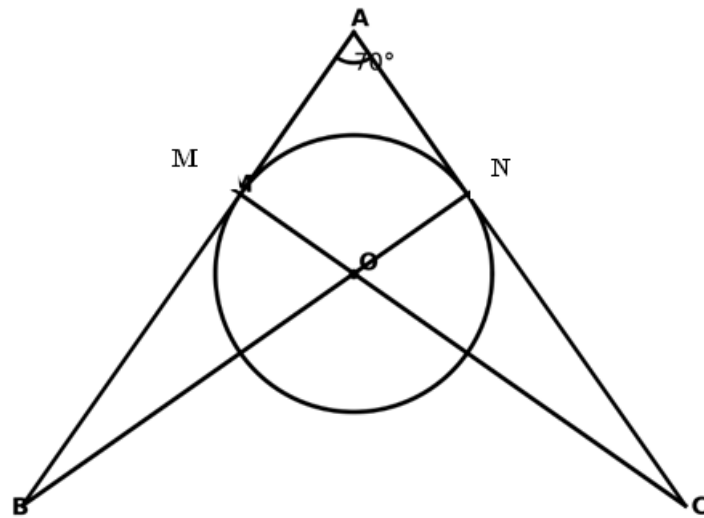
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22.



Points M and N lie on a circle with centre O.
 The lines AM and AN are tangents to the circle at M and N.
 The line through N and O meets the tangent AM at B.
 The line through M and O meets the tangent AN at C.
 Given that $\angle MAN = 70^\circ$.
 Prove that $\triangle ABN$ and $\triangle ACM$ are congruent.
 Give a reason for each step.

(4)



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23.

Express as a single fraction in its simplest form

$$\frac{1}{x^2 - 4x + 3} \div \left(\frac{3}{x^2 - 9} - \frac{5}{x - 3} \right)$$

(3)

24.

Find the set of possible values of x for which

$$6x^2 - 14x - 12 \leq 0 \text{ and } 4x^2 + 2x > 30$$

(3)

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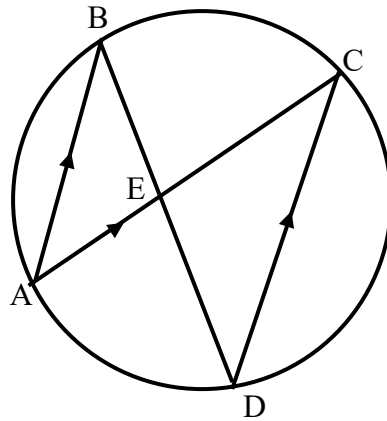
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25.



A, B, C, D are points on a circle. The diagonals AC and BD intersect at E.
You are given the vectors:

$$\overrightarrow{AB} = 2a, \overrightarrow{AE} = b, \overrightarrow{DC} = 3a.$$

Find \overrightarrow{ED} in terms of a and b.

(5)

END

TOTAL FOR PAPER IS 80 MARKS

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GCSE Level Maths Predicted Papers 2026 (May): Paper 1: Set 1:

Answers

1.

$$\boxed{250 = 2 \times 5^3}$$

2.

(a) Find the final velocity v

$$v^2 = (\sqrt{20})^2 + 2(2)(4)$$

$$v^2 = 20 + 16 = 36$$

$$v = \sqrt{36} = 6$$

$$\boxed{v = 6 \text{ m/s}}$$

(b) Make a the subject

$$v^2 = u^2 + 2as$$

$$v^2 - u^2 = 2as$$

$$a = \frac{v^2 - u^2}{2s}$$

$$\boxed{a = \frac{v^2 - u^2}{2s}}$$

3.

Find total weight of each colour

- Red balls: $3 \times 6 = 18\text{kg}$
- Blue balls: $4 \times 8 = 32\text{kg}$
- Green balls: $2 \times 5 = 10\text{kg}$

Find total weight of all balls

$$18 + 32 + 10 = 60 \text{ kg}$$

$$\text{Mean} = \frac{60}{9} = 6.\bar{6} \text{ kg} \approx 6.67 \text{ kg}$$

Since $6.67 < 7$, Sam is correct.

4.

(a) Any non-zero expression raised to the power 0 equals 1.

$$(3q)^0 = \boxed{1}$$

(c) When multiplying powers with the same base, add the indices:

$$x^7 \times x^{-4} = x^{7+(-4)} = x^3$$

$$\boxed{m = 3}$$

(d) Apply the power to each factor:

$$\begin{aligned} (4b^3c^2)^2 &= 4^2 \cdot b^{3 \times 2} \cdot c^{2 \times 2} \\ &= 16b^6c^4 \end{aligned}$$

$$\boxed{16b^6c^4}$$

5.

The equation of L_1 is in the form $y = mx + c$, so the gradient is:

$$m_1 = -3$$

Rearrange $4y + px - 8 = 0$ into the form $y = mx + c$:

$$4y = -px + 8$$

$$y = -\frac{p}{4}x + 2$$

$$m_2 = -\frac{p}{4}$$

For two lines to be perpendicular:

$$m_1 \times m_2 = -1$$

$$(-3)\left(-\frac{p}{4}\right) = -1$$

$$\frac{3p}{4} = -1$$

$$p = -\frac{4}{3}$$

6.

$$\left(\frac{\sin 60 \times \tan 30}{2 \sin 30}\right)^4$$

$$= \left(\frac{\sqrt{\frac{3}{2}} \times \frac{1}{\sqrt{3}}}{2 \times \frac{1}{2}}\right)^4$$

$$= 1/16$$

7.

First simplify the numerator:

$$(\sqrt{12} + \sqrt{3})^2 = 12 + 3 + 2\sqrt{36} = 15 + 12 = 27.$$

So the expression becomes

$$\frac{27}{\sqrt{6} - \sqrt{2}}$$

Rationalise the denominator by multiplying top and bottom by $\sqrt{6} + \sqrt{2}$:

$$\frac{27(\sqrt{6} + \sqrt{2})}{(\sqrt{6} - \sqrt{2})(\sqrt{6} + \sqrt{2})} = \frac{27(\sqrt{6} + \sqrt{2})}{6 - 2} = \frac{27(\sqrt{6} + \sqrt{2})}{4}$$

8.(a)

$$\frac{8x + 3(x + 2)}{2x(x + 2)}$$

$$\frac{8x + 3x + 6}{2x(x + 2)} = \frac{11x + 6}{2x(x + 2)}$$



$$\frac{11x + 6}{2x(x + 2)}$$

(b)

Take out the common factor $(x + 3y)$:

$$\begin{aligned} &(x + 3y)^2 + 5(x + 3y) \\ &= (x + 3y)((x + 3y) + 5) \\ &\boxed{(x + 3y)(x + 3y + 5)} \end{aligned}$$

9.

Convert 36 minutes to hours:

$$36 \text{ min} = \frac{36}{60} = 0.6 \text{ h}$$

Distance = speed \times time:

$$100 \times 0.6 = 60$$

$$\boxed{60 \text{ km}}$$

(b) Is Liam correct?

Convert 100 km/h to m/s:

$$100 \text{ km/h} = \frac{100\,000}{3600} \text{ m/s} \approx 27.8 \text{ m/s}$$

Compare with 50 m/s:

$$27.8 < 50$$

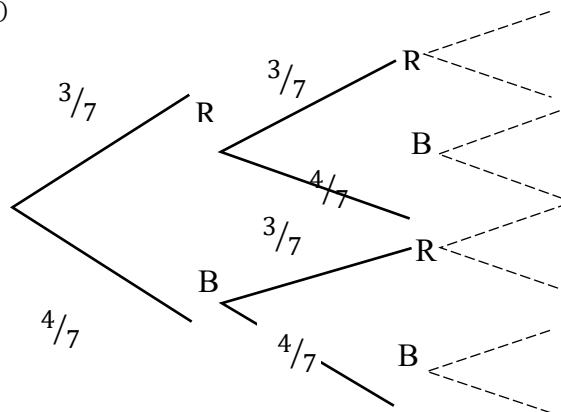
So 100 km/h is slower than 50 m/s.

$\boxed{\text{No, Liam is not correct.}}$

10.

Probability $\Rightarrow 1 - P(\text{all red}) - P(\text{all blue})$

$$\Rightarrow 1 - \left(\frac{3}{7}\right)^n - \left(\frac{4}{7}\right)^n$$



11.

For similar shapes:

- Surface area ratio = 9:16
- Linear scale factor = $\sqrt{\frac{9}{16}} = \frac{3}{4}$ (C to D)

Volume ratio is the cube of the linear scale factor:

$$\text{Volume ratio } C:D = \left(\frac{3}{4}\right)^3 = \frac{27}{64}$$

So tank D is:



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$$\frac{64}{27}$$

times the volume of tank C.

That means Aisha must fill tank C:

$$\frac{64}{27}$$

Final answer: $2\frac{10}{27}$ times: 3 times

12.

$$Y = 12 + 6px - 2x^2$$

$$Y = -2(x^2 - 3px - 6)$$

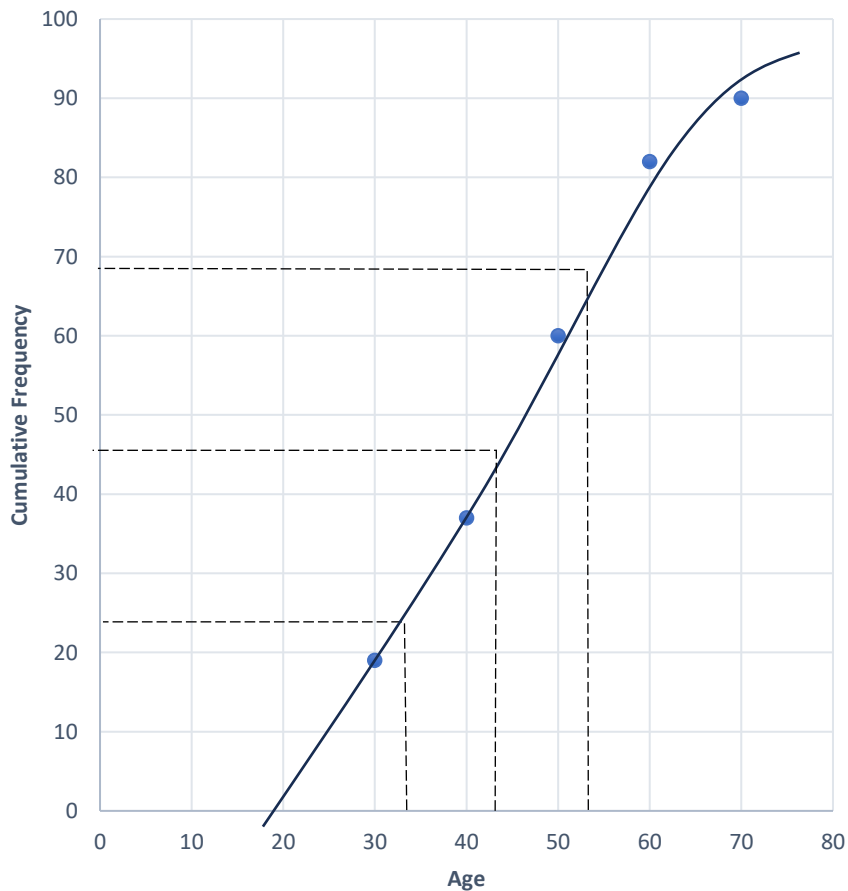
$$= -2 \left[\left(x - \frac{3p}{2}\right)^2 - \left(\frac{3p}{2}\right)^2 - 6 \right]$$

$$= -2 \left[\left(x - \frac{3p}{2}\right)^2 - \left(\frac{9p^2 + 24}{4}\right) \right]$$

$$= -2 \left(x - \frac{3p}{2}\right)^2 + \frac{9p^2 + 24}{2}$$

Max. point $\left(\frac{3p}{2}, \frac{9p^2 + 24}{4}\right)$

13.a)



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b)

$$\text{median} \rightarrow 90 \times \frac{1}{2} = 45^{\text{th}} \Rightarrow 43$$

$$\text{U.Q} \Rightarrow 90 \times \frac{3}{4} \Rightarrow 67.5 \Rightarrow 54$$

$$\text{L.Q} \Rightarrow 90 \times \frac{1}{4} \Rightarrow 22.5 \Rightarrow 33$$

$$\left. \begin{array}{l} \text{U.Q} \Rightarrow 90 \times \frac{3}{4} \Rightarrow 67.5 \Rightarrow 54 \\ \text{L.Q} \Rightarrow 90 \times \frac{1}{4} \Rightarrow 22.5 \Rightarrow 33 \end{array} \right\} \begin{array}{l} \text{I. Q. R} = 54 - 33 \\ = 21 \end{array}$$

14.

a) Find missing values

Find Upper Quartile Q3

$$Q3 = Q1 + IQR = 50 + 10 = 60$$

Find Maximum

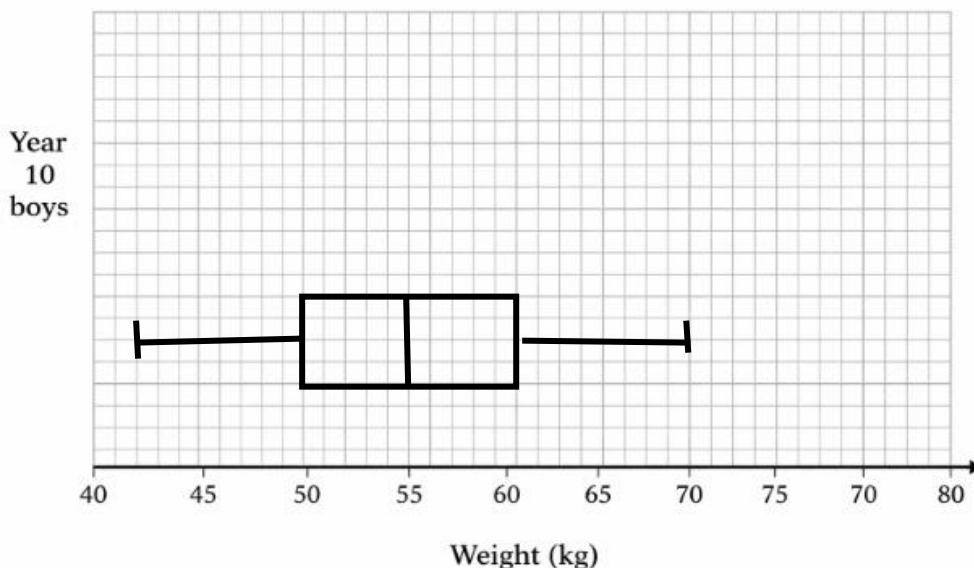
$$\text{Maximum} = \text{Smallest} + \text{Range} = 42 + 28 = 70$$

Five-number summary:

- Minimum = 42
- Q1 = 50
- Median = 55
- Q3 = 60
- Maximum = 70

Box plot (what you draw)

- Box from 50 to 60
- Median line at 55
- Whiskers to 42 and 70



(b) Comparison (model answer)

Answer:

- The medians are similar (both around mid-50s)
- The Year 8 boys have a larger range, so their weights are more spread out

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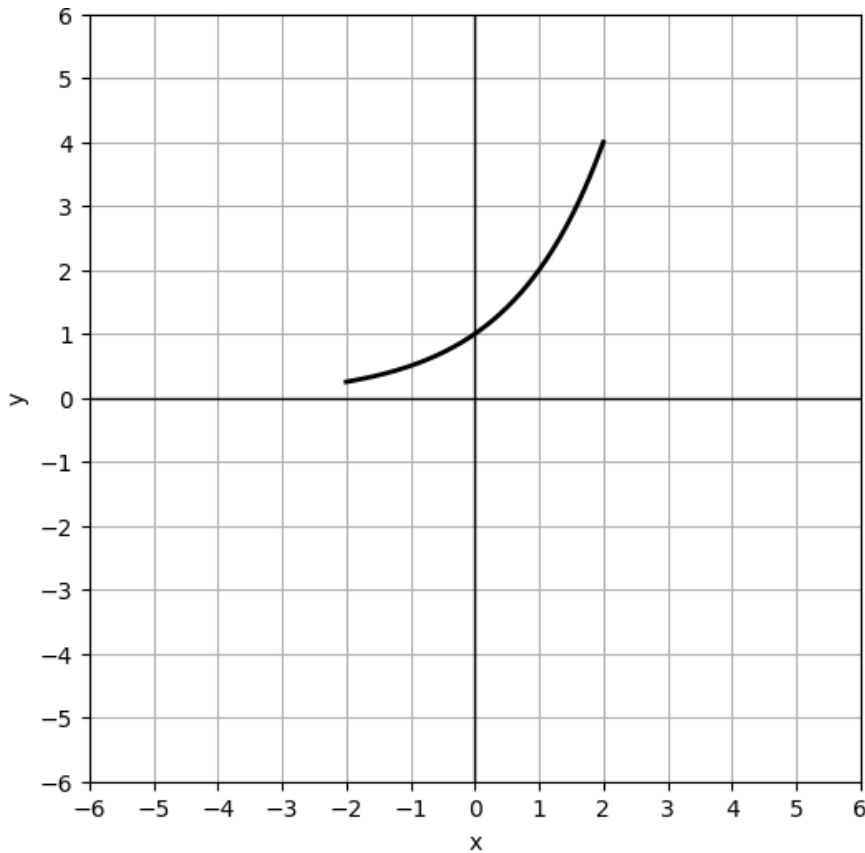
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- The Year 10 boys have a smaller spread (IQR = 10), so their weights are more consistent

15. (a)



(b) Find a and b if $y = ab^x$ passes through $(1,8)$ and $(4,64)$

From $(1,8)$:

$$8 = ab^1 \Rightarrow ab = 8$$

From $(4,64)$:

$$64 = ab^4$$

Divide the second equation by the first:

$$\frac{64}{8} = \frac{ab^4}{ab} = b^3$$

$$8 = b^3 \Rightarrow b = 2$$

Now use $ab = 8$:

$$a(2) = 8 \Rightarrow a = 4$$

$$\boxed{a = 4, b = 2}$$



16.

$$\frac{\text{Area of the base of the cone}}{\text{Total surface area of the cone}} = \frac{\sqrt{3}}{2 + \sqrt{3}} = \frac{\pi r^2}{\pi r^2 + \pi r l}$$

$$\frac{r^2}{r^2 + r l} = \frac{\sqrt{3}}{2 + \sqrt{3}}$$

$$r^2(2 + \sqrt{3}) = (r^2 + r l)\sqrt{3}$$

$$2r^2 = \sqrt{3} r l$$

$$r = \frac{\sqrt{3}}{2} l$$

$$\sin \theta = \frac{r}{l}$$

$$= \frac{\sqrt{3}/2 l}{l}$$

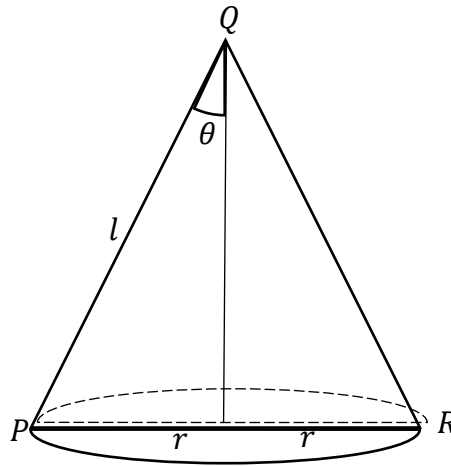
$$\sin \theta = \sqrt{3}/2$$

$$\sin \theta = \sin 60^\circ$$

$$P\hat{Q}R = 2\theta$$

$$= \frac{2\pi}{3}$$

$$= 120^\circ$$



17.

(a)

To show that $f^{-1}(20) = 36$, we check that $f(36) = 20$.

$$\begin{aligned} f(36) &= 3\sqrt{36} + 2 \\ &= 3(6) + 2 \\ &= 18 + 2 = 20 \end{aligned}$$

Since $f(36) = 20$, it follows that:

$$\boxed{f^{-1}(20) = 36}$$

(b)

Find the values of x for which $hg(x) = 2$

First find the composite function:

$$hg(x) = h(g(x)) = h(x + 1) = 2(x + 1)^2.$$

$$2(x + 1)^2 = 2$$

$$(x + 1)^2 = 1$$

$$x + 1 = \pm 1.$$

$$x = 0 \text{ or } x = -2.$$

18.

Original graph:

$$y = \tan x^\circ$$

Point $P(180,0)$ moves to point $Q(280,6)$

Horizontal movement

$$250 - 280 = 100$$

Vertical movement

$$6 - 0 = 6$$

$$h(x) = \tan(x - 100)^\circ + 6$$

19.

$$x = 0.3\dot{5}$$

$$y = 0.5\dot{5} = 0.\dot{5} - \textcircled{3}$$

$$10x = 3.\dot{5} - \textcircled{1}$$

$$10y = 5.\dot{5} - \textcircled{4}$$

$$100x = 35.\dot{5} - \textcircled{2}$$

$$\textcircled{4} - \textcircled{3} \Rightarrow 9y = 5$$

$$\textcircled{2} - \textcircled{1} \Rightarrow 90x = 32$$

$$y = \frac{5}{9}$$

$$x = \frac{32}{90}$$

$$\Rightarrow x/y = \frac{32/90}{5/9} = \frac{32}{50} = \frac{16}{25}$$

20.

$$k \propto \frac{1}{p^2}$$

$$k = \frac{m}{p^2}$$

$$\text{When } \left(\begin{matrix} k=1 \\ p=\sqrt{7} \end{matrix} \right) \Rightarrow 1 = \frac{m}{(\sqrt{7})^2}$$

$$m = 1 \times 7 = 7$$

$$\text{Equation } \Rightarrow k = \frac{7}{p^2}$$

$$p = 10$$

$$k = \frac{7}{100} = 0.07$$

21.

Let the radius of the sphere be r .

$$\frac{2}{5} \times 4\pi r^2 = 32\pi$$

$$\frac{8}{5}\pi r^2 = 32\pi$$

$$r^2 = 32 \times \frac{5}{8} = 20$$

$$r = \sqrt{20} = \sqrt{4 \times 5} = 2\sqrt{5}$$

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22.

1. $\angle ANB = 90^\circ$

Reason: A radius is perpendicular to a tangent at the point of contact.

(ON is a radius and AN is tangent at N ; also B lies on line ON , so NB is along ON .)

2. $\angle AMC = 90^\circ$

Reason: A radius is perpendicular to a tangent at the point of contact.

(OM is a radius and AM is tangent at M ; also C lies on line OM , so MC is along OM .)

3. $AN = AM$

Reason: Tangents from the same external point are equal in length.

4. $\angle BAN = \angle CAM$

Reason: They are the same angle formed by the same two lines AM and AN .

(B lies on AM , C lies on AN , so $\angle BAN$ is the angle between AM and AN , and $\angle CAM$ is also the angle between AN and AM .)

5. Therefore, $\triangle ABN \cong \triangle ACM$

Reason: ASA congruence (two equal angles and the included side:

$\angle ANB = \angle AMC$, $AN = AM$, and $\angle BAN = \angle CAM$).

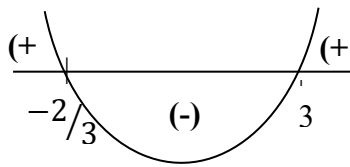
23.

$$\begin{aligned} & \frac{1}{x^2-4x+3} \div \left(\frac{3}{x^2-9} - \frac{5}{x-3} \right) \\ \Rightarrow & \frac{1}{(x-3)(x-1)} \div \left(\frac{3}{(x-3)(x+3)} - \frac{5}{(x-3)} \right) \\ \Rightarrow & \frac{1}{(x-3)(x-1)} \div \left(\frac{3-5(x+3)}{(x-3)(x+3)} \right) \\ \Rightarrow & \frac{1}{(x-3)(x-1)} \div \left(\frac{-5x-12}{(x-3)(x+3)} \right) \\ \Rightarrow & \frac{1}{(x-3)(x-1)} \times \left(\frac{(x-3)(x+3)}{-(5x+12)} \right) \\ \Rightarrow & \frac{-(x+3)}{(x-1)(5x+12)} \end{aligned}$$

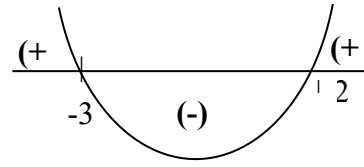
24.

$$\begin{array}{ll} 6x^2 - 14x - 12 \leq 0 & \text{or} \quad 4x^2 + 2x > 30 \\ 6x^2 - 14x - 12 \leq 0 & \text{or} \quad 2x(2x + 1) > 30 \\ 2(3x^2 - 7x - 6) \leq 0 & \text{or} \quad x(2x + 1) > 15 \\ 2(3x + 2)(x - 3) \leq 0 & \text{or} \quad 2x^2 + x - 15 > 0 \\ 2(3x + 2)(x - 3) \leq 0 & \text{or} \quad (2x - 5)(x + 3) > 0 \end{array}$$

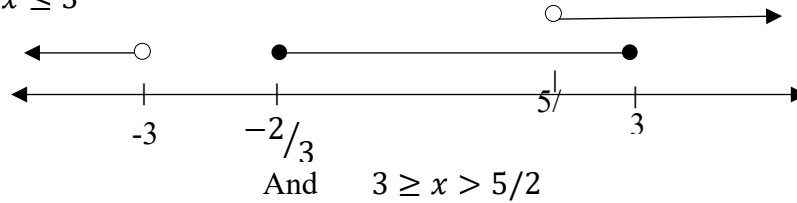




$$-\frac{2}{3} \leq x \leq 3$$



$$-3 > x \text{ or } x > \frac{5}{2}$$



25.

Identify two triangles

Consider triangles:

- $\triangle AEB$
- $\triangle CED$

Show the triangles are similar

- $\angle AEB = \angle CED$ (vertically opposite angles, since AC and BD intersect at E)
- $\angle ABE = \angle CDE$ (alternate/corresponding angles because $AB \parallel DC$ and BE is the same line as DE)

$$\triangle AEB \sim \triangle CED$$

Use corresponding side ratios

From similarity:

$$\frac{AB}{DC} = \frac{AE}{EC}$$

Substitute $AB = 2a$ and $DC = 3a$ (same direction, parallel):

$$\frac{AB}{DC} = \frac{2}{3}$$

$$\frac{AE}{EC} = \frac{2}{3} \Rightarrow EC = \frac{3}{2}AE$$

Given $\vec{AE} = b$, and E lies on AC so \vec{EC} is in the same direction as \vec{AE} ,

$$\vec{EC} = \frac{3}{2}b$$

$$\vec{ED} = \vec{EC} + \vec{CD} = \frac{3}{2}b - 3a$$

END

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GCSE Maths Predicted Paper 2

2026 (June): Calculator

Set 1

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GCSE Maths Predicted Paper 2026 (June)
Paper 2: Calculator (Set 1)
Duration: 1 hour and 30 minutes

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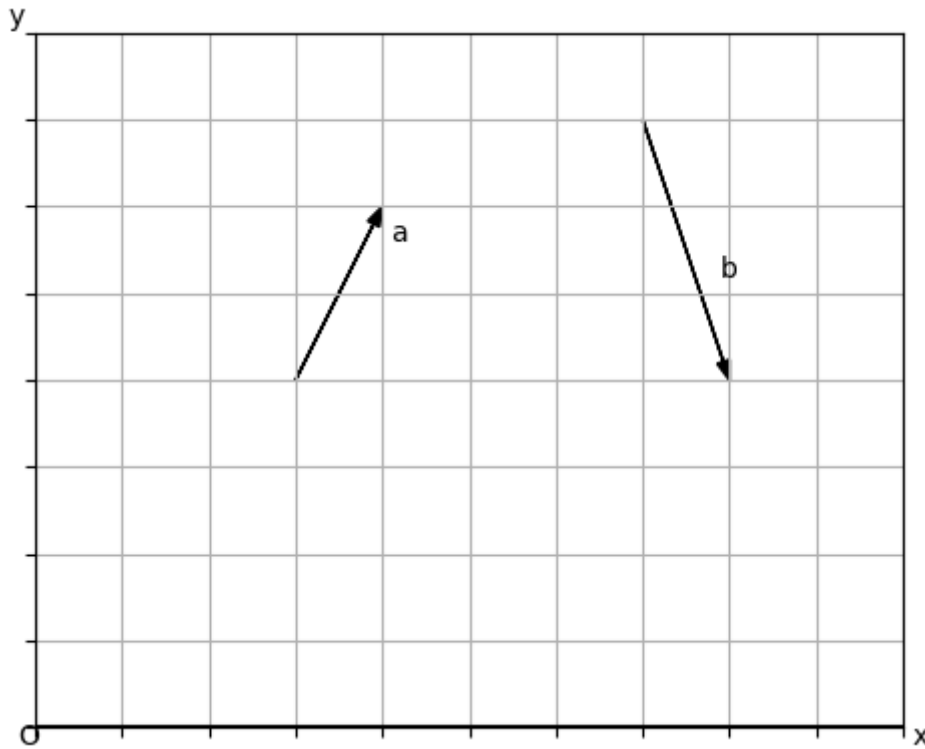
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Grade Boundary: Grade 8: 70% and Grade 9: 82%

3.

The vector a and the vector b are shown on the grid



- (a) On the grid, draw and label the vector $-1.5a$.
- (b) Work out $3a + 4b$ as a column vector.

(3)

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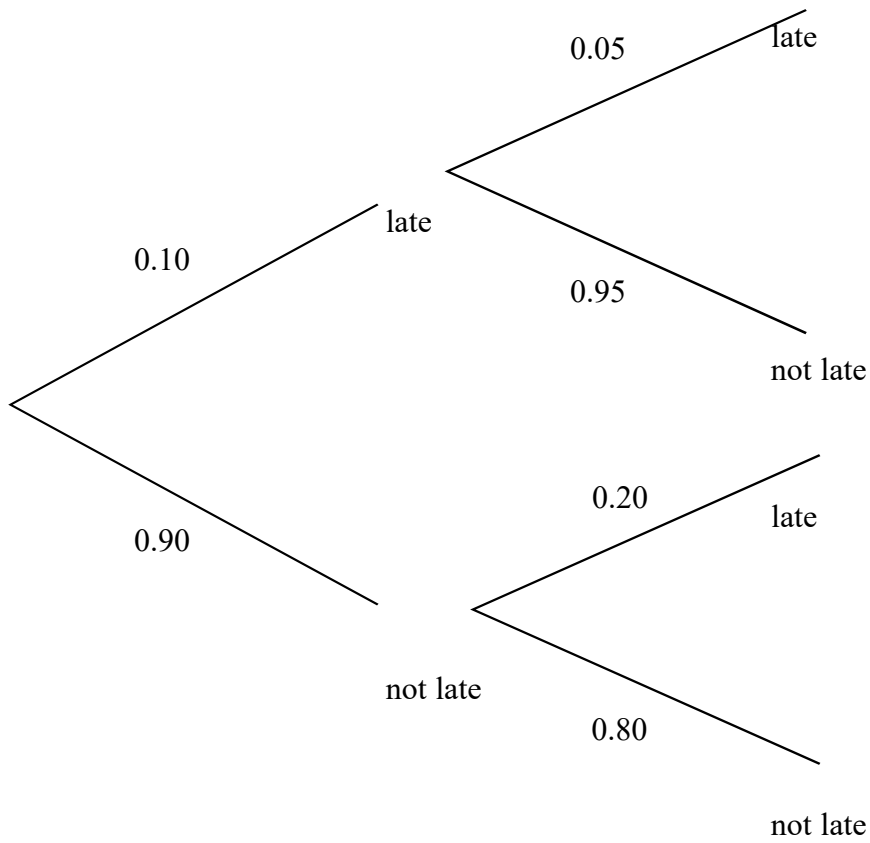
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6.

The probability tree diagram shows the probabilities that Peter will be late for work on two days next week.



Calculate the probability that Peter will be late on exactly one of the two days.

(2)



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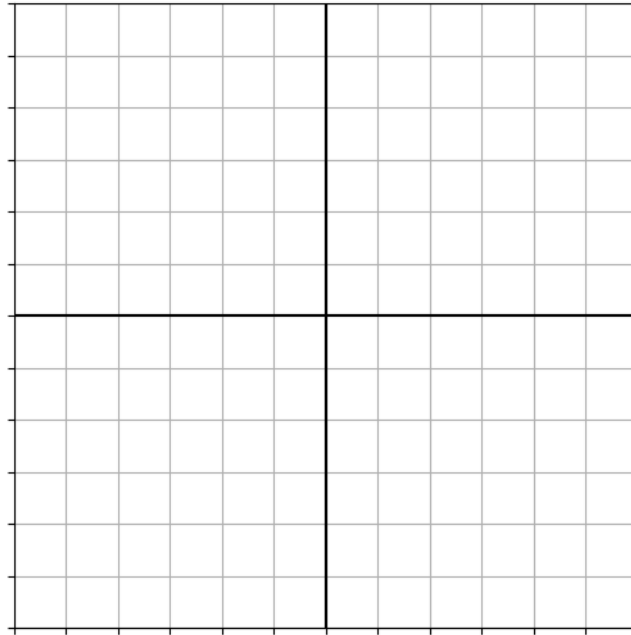
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(a) On the grid below, draw the graph of

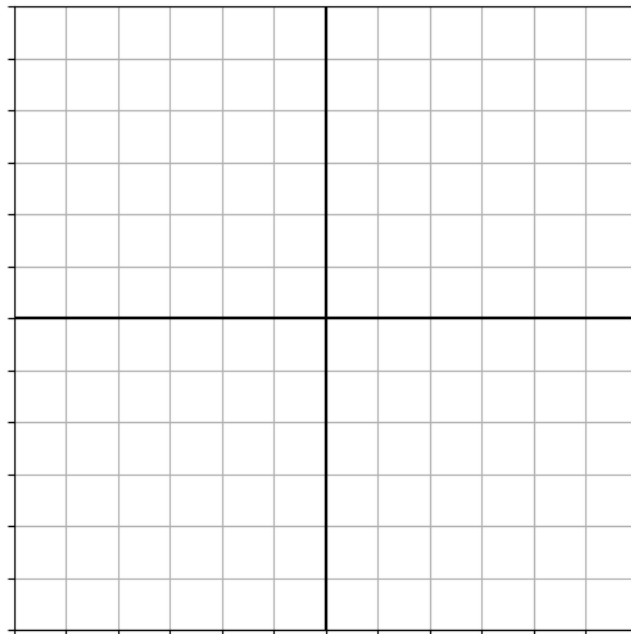
$$y = f(x) - 2.$$



(b)

On the grid below, draw the graph of

$$y = f(-x).$$



(2)



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14.

Aamir invested £4200 for 4 years.

- He was paid 3.1% compound interest for each of the first 3 years.
- He was paid $R\%$ interest for the fourth year.

At the end of 4 years he had £4867.67.

Find R . Give your answer correct to 1 decimal place.

(3)

15.

The n^{th} term of a sequence is given by $pn^2 + qn$ where a and b are integers. The

2^{nd} term of the sequence is 2 and the 4^{th} term of the sequence is 10

(a) Find the 5^{th} term of the sequence.

(b) Here are the first 5 terms of a different quadratic sequence find the n^{th} term of this sequence

0 4 12 24 40

(4)

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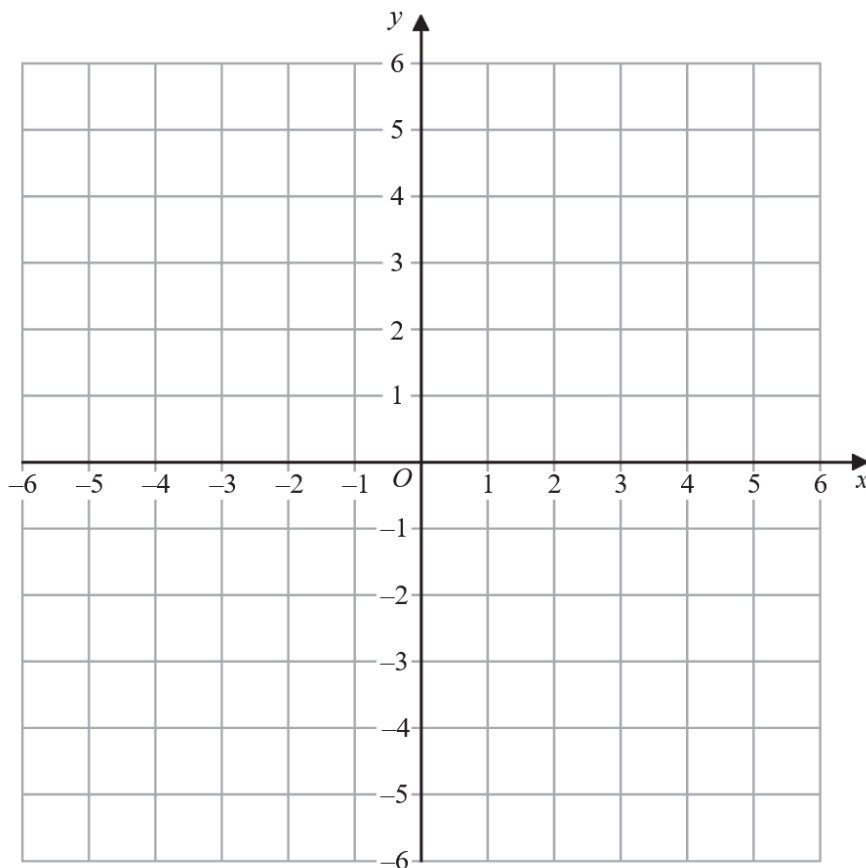


16.

(a) Complete the table of values for $y = 2x^2 - 2x - 3$

x	-2	-1	0	0	2	3
y						

(b) On the grid, draw the graph of $y = 2x^2 - 2x - 3$ for values of x from -2 to 3



(c) Use your graph to find estimates of the solutions of the equation

$$x^2 + 2x - 1 = 0$$

(4)



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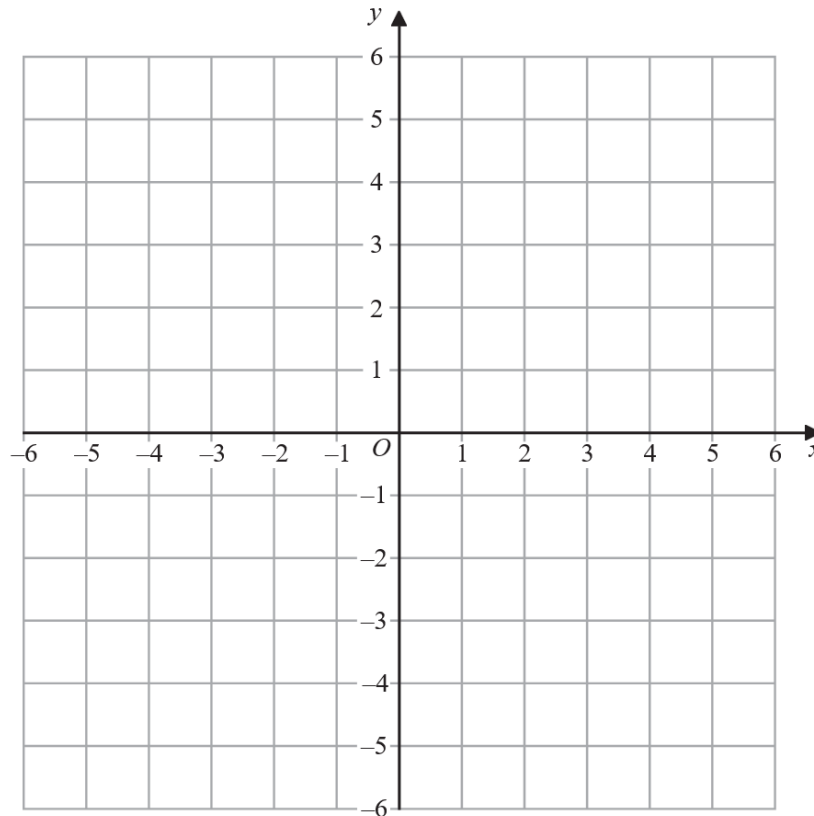
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19.

a) On the grid, construct the graph of $x^2 + y^2 = 25$



b) Using part (a), find estimates for the solutions of the simultaneous equations.

$$x^2 + y^2 = 25$$

$$y = -2x + 3$$

(4)

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20.

James is ordering a new laptop.

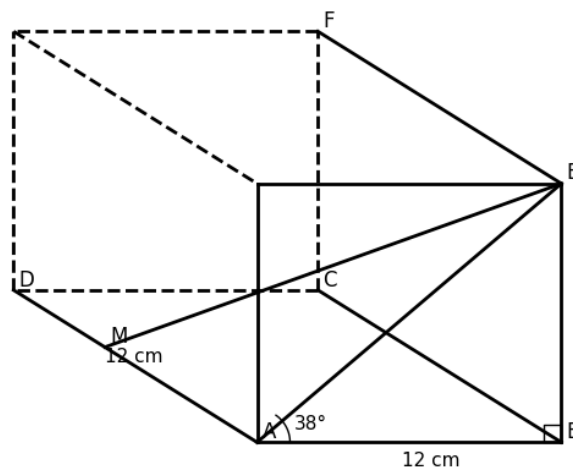
He can choose:

- 12 different laptop colours
- 18 different storage options
- a number of different keyboard layouts

The total number of different laptops James can order is 4320.

Work out the number of different keyboard layouts James can choose from. (3)

21.



A triangular prism has a square base $ABCD$ of side length 12 cm.

- $\angle ABE$ and $\angle CBE$ are right angles.
- $\angle EAB = 38^\circ$.
- M is on DA such that

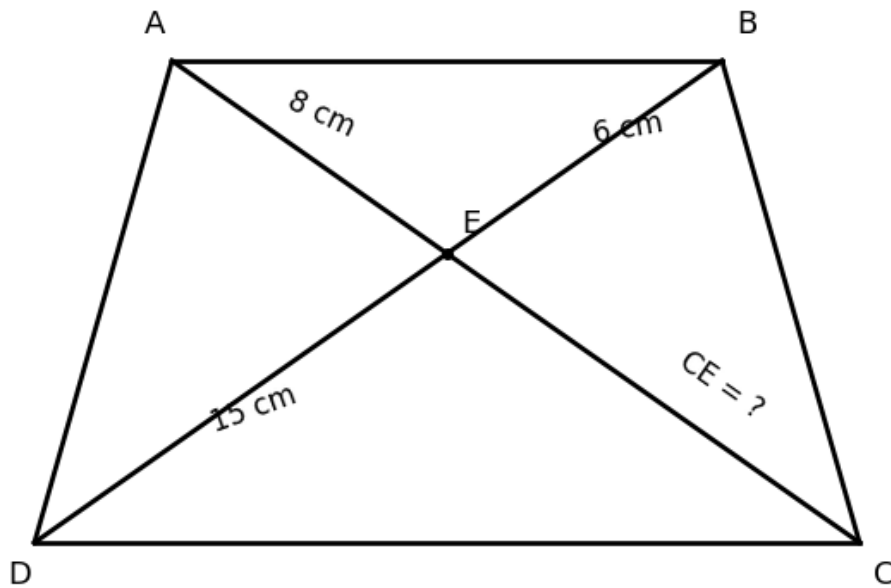
$$DM : MA = 3 : 5$$

Calculate the angle between EM and the base of the prism.

(5)



23.



Shape $ABCD$ is a trapezium with $AB \parallel DC$. Diagonals AC and BD intersect at E .

Given:

- $AE = 8\text{ cm}$
- $EB = 6\text{ cm}$
- $DE = 15\text{ cm}$

Find CE .

(3)

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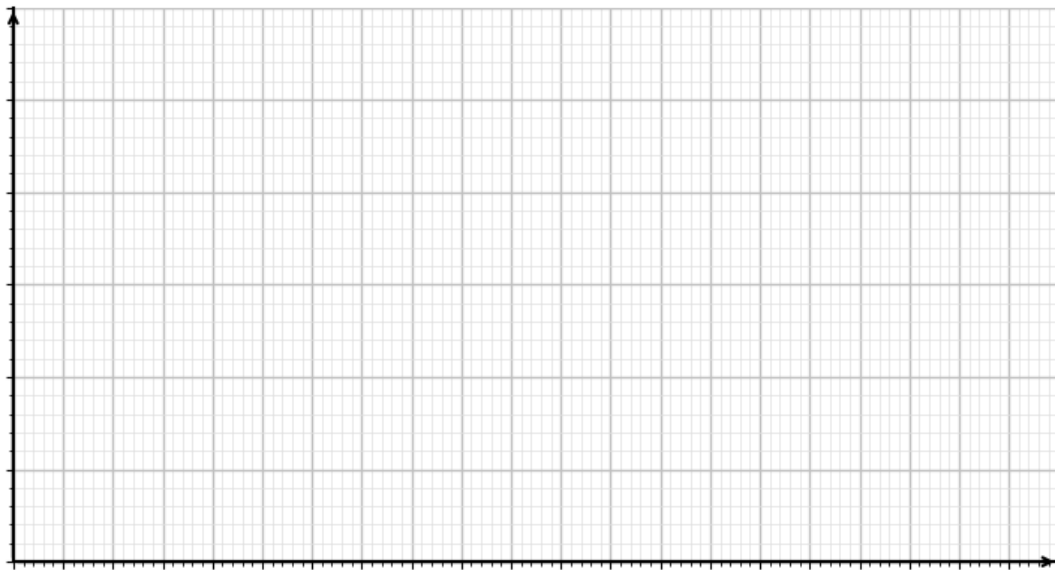


24.

The table gives information about the widths w metres, of trees in some wood.

Width (w m)	Frequency
$0 < h \leq 3$	3
$3 < h \leq 4$	4
$4 < h \leq 7$	15
$7 < h \leq 15$	24
$15 < h \leq 21$	12

Draw a histogram to show this information.



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GCSE Level Maths Predicted Paper 2: 2026 (June) Set 1:

Answers

1.

0.240

2.

$$65\% \text{ of } 1\,200 = 0.65 \times 1\,200 = 780 \text{ kg}$$

Plastic : Metal = 5 : 3

Total parts = 5 + 3 = 8

Each part:

$$780 \div 8 = 97.5 \text{ kg}$$

Step 3: Find the weight of metal

$$\text{Metal} = 3 \times 97.5 = 292.5 \text{ kg}$$

3.

(a) Draw and label the vector $-1.5a$

First calculate $-1.5a$:

$$-1.5a = -1.5 \begin{pmatrix} 1 \\ 2 \end{pmatrix} = \begin{pmatrix} -1.5 \\ -3 \end{pmatrix}.$$

How to draw it on the grid

- From any point, move 1.5 units left
- Then move 3 units down
- Draw the arrow and label it $-1.5a$

(b) Work out $3a + 4b$ as a column vector

Find $3a$

$$3a = 3 \begin{pmatrix} 1 \\ 2 \end{pmatrix} = \begin{pmatrix} 3 \\ 6 \end{pmatrix}.$$

Find $4b$

$$4b = 4 \begin{pmatrix} 1 \\ -3 \end{pmatrix} = \begin{pmatrix} 4 \\ -12 \end{pmatrix}.$$

Add the vectors

$$3a + 4b = \begin{pmatrix} 3 \\ 6 \end{pmatrix} + \begin{pmatrix} 4 \\ -12 \end{pmatrix} = \begin{pmatrix} 7 \\ -6 \end{pmatrix}.$$

4.

$$\text{Area} = \frac{\theta}{360} \pi r^2$$

$$75 = \frac{\theta}{360} \pi (10)^2$$

$$\theta \approx 85.9^\circ$$

$$\text{Arc length} = \frac{\theta}{360} \cdot 2\pi r$$

$$= \frac{85.9}{360} \cdot 2\pi(10)$$

$$\approx 14.99 \text{ cm}$$

Perimeter = arc length + two radii:

$$P = 14.99 + 2(10) = 34.99 \text{ cm}$$



5.

$$\text{Pressure} = \frac{\text{force}}{\text{area}}$$

Original pressure

$$P_1 = \frac{60}{15} = 4$$

New pressure

$$P_2 = \frac{75}{20} = 3.75$$

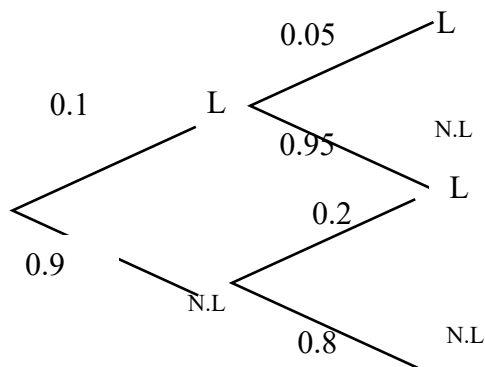
Decrease in pressure

$$4 - 3.75 = 0.25$$

$$\frac{0.25}{4} \times 100 = 6.25\%$$

Since $6.25\% < 10\%$, the student is not correct.

6.



$$\begin{aligned} \text{Not late exactly one day} &\Rightarrow 0.1 \times 0.95 + 0.9 \times 0.2 \\ &\Rightarrow 0.095 + 0.18 \\ &\Rightarrow 0.275 \end{aligned}$$

7.

$$\begin{aligned} k(2n^2 + 7) &= 5n^2 - 3. \\ 2kn^2 + 7k &= 5n^2 - 3. \\ 2kn^2 - 5n^2 &= -3 - 7k \\ n^2(2k - 5) &= -(7k + 3). \end{aligned}$$

$$n^2 = \frac{-(7k + 3)}{2k - 5} = \frac{7k + 3}{5 - 2k}.$$

$$n = \pm \sqrt{\frac{7k + 3}{5 - 2k}}$$

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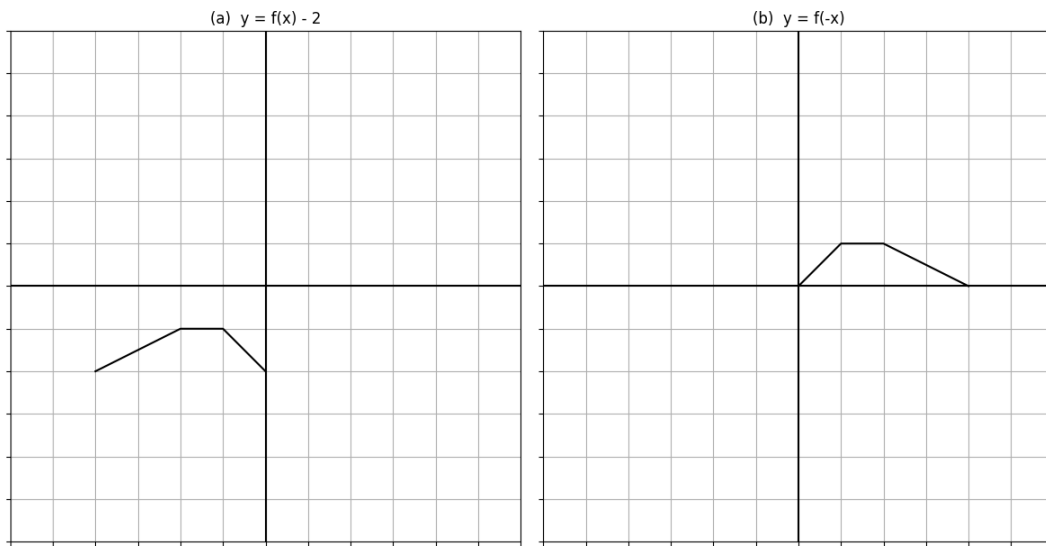
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8.



9.

$$1.998 \times 10^{-4}$$

10.

	Small	:	large
Area ratio	= 9	:	16
Volume ratio	= $(\sqrt{9})^3$:	$(\sqrt{16})^3$
	= 27	:	64

Therefore, large volume = $\frac{250}{27} \times 64 = 592.6 \text{ cm}^3$

11.

$$3a : 4c = 9 : 16$$

$$\frac{3a}{4c} = \frac{9}{16}$$

$$a = \frac{3}{4}c$$

$$5b : 6c = 25 : 24$$

$$\frac{5b}{6c} = \frac{25}{24}$$

$$b = \frac{5}{4}c$$

$$a + b = \frac{3}{4}c + \frac{5}{4}c = \frac{8}{4}c = 2c$$

$$b + c = \frac{5}{4}c + c = \frac{9}{4}c$$

$$a + b : b + c = 2c : \frac{9}{4}c$$

$$\boxed{a + b : b + c = 8 : 9}$$

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12.

$$a = \sin x, b = \sin y.$$

Then the equations become:

$$6a + 2b = 3(1)$$

$$3a - 4b = -3(2)$$

$$12a + 4b = 6(3)$$

$$15a = 3$$

$$a = \frac{1}{5}$$

$$\sin x = \frac{1}{5}$$

$$6\left(\frac{1}{5}\right) + 2b = 3$$

$$b = \frac{9}{10}$$

$$\sin y = \frac{9}{10}$$

$$x = \sin^{-1}\left(\frac{1}{5}\right) \approx 11.54^\circ$$

$$y = \sin^{-1}\left(\frac{9}{10}\right) \approx 64.16^\circ$$

$$\boxed{x \approx 11.5^\circ, y \approx 64.2^\circ}$$

13.

1) Write the bounds for BC and AC

$$BC = 11.2 \text{ cm}$$

$$11.15 \leq BC < 11.25$$

$$AC = 13.9 \text{ cm}$$

$$13.85 \leq AC < 13.95$$

$$\cos x_{\min} = \frac{11.25}{13.85} = 0.812274 \dots$$

$$x_{\min} = \cos^{-1}(0.812274 \dots) = 35.681 \dots^\circ$$

$$\boxed{x_{\min} \approx 35.7^\circ}$$

$$\cos x_{\max} = \frac{11.15}{13.95} = 0.799283 \dots$$

$$x_{\max} = \cos^{-1}(0.799283 \dots) = 36.938 \dots^\circ$$

$$\boxed{x_{\max} \approx 36.9^\circ}$$

$$\boxed{35.7^\circ \leq x < 36.9^\circ}$$

14.

After 3 years:

$$4200(1.031)^3$$

$$(1.031)^3 \approx 1.095939$$

$$\text{Amount after 3 years} \approx 4200 \times 1.095939 = 4602.94$$

Final amount:



$$4602.94\left(1 + \frac{R}{100}\right) = 4867.67$$

$$1 + \frac{R}{100} = \frac{4867.67}{4602.94} = 1.05750$$

$$\frac{R}{100} = 0.05750 \Rightarrow R = 5.750$$

$$\boxed{R = 5.8\% \text{ (1 d.p.)}}$$

15.

$$\text{nth term} \Rightarrow pn^2 + qn$$

$$n = 2 / \quad 2 = p2^2 + 2q$$

$$1 = 2p + q - \textcircled{1}$$

$$n = 4 / \quad 10 = p(4)^2 + 4q$$

$$10 = 16p + 4q$$

$$5 = 8p + 2q - \textcircled{2}$$

$$\textcircled{1} \times 2 \Rightarrow 2 = 4p + 2q - \textcircled{3}$$

$$\textcircled{2} - \textcircled{3} \Rightarrow 3 = 4p$$

$$p = \frac{3}{4}$$

$$\text{Equation} \Rightarrow \frac{3}{4}n^2 - \frac{1}{2}n$$

$$\text{a) } n = 5 / \quad \frac{3}{4}(5)^2 - \frac{1}{2}(5)$$

$$\Rightarrow \frac{75}{4} - \frac{5}{2} = \frac{65}{4}$$

$$\text{b) } 0, 4, 12, 24, 40$$

$$2a = 4$$

$$a = 2$$

$$3a + b = 4$$

$$6 + b = 4$$

$$b = (-2)$$

$$a + b + c = 0$$

$$2 + (-2) + c = 0$$

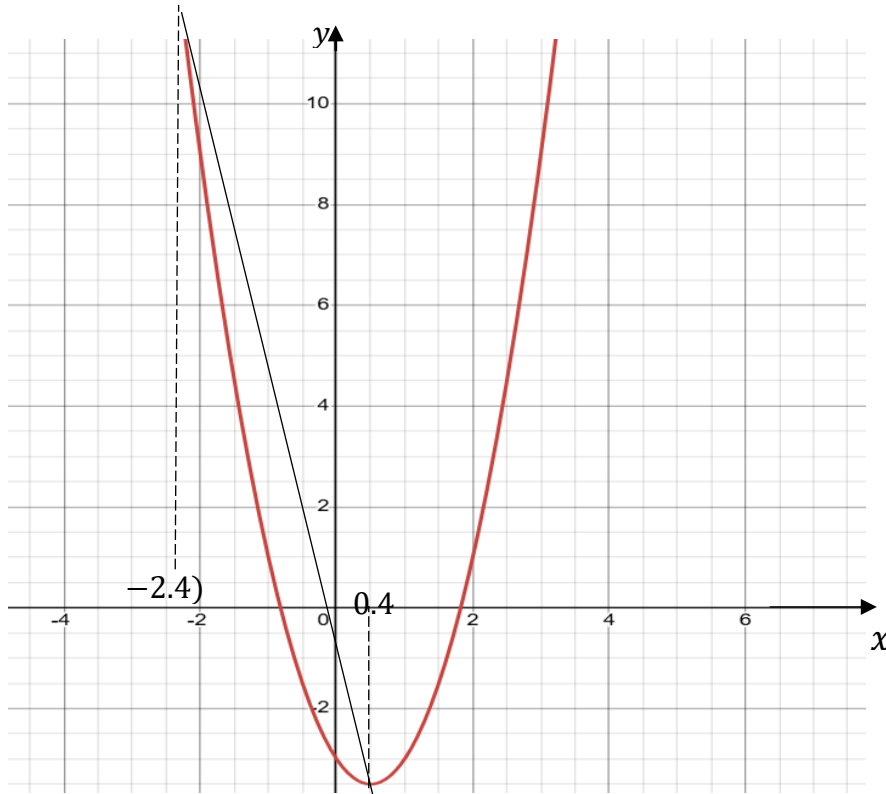
$$\Rightarrow 2n^2 - 2n$$

16.

a)

x	-2	-1	0	0	2	3
y	9	1	-3	-3	1	9

b)



$$y = -6x - 1$$

x	0	-1
y	-1	5

$$\begin{aligned} x^2 + 2x - 1 &= 0 \\ 2x^2 + 4x - 2 &= 0 \quad (1) \\ 2x^2 - 2x - 3 &= y \quad (2) \\ (2) - (1) \quad -6x - 1 &= y \\ \text{Solutions } \Rightarrow x &= 0.4, -2.4 \end{aligned}$$

17.

Rearrange:

$$20x^2 - 7xy - 6y^2 = 0$$

Divide the whole equation by y^2

$$20\left(\frac{x}{y}\right)^2 - 7\left(\frac{x}{y}\right) - 6 = 0$$

$$\left(5\frac{x}{y} + 2\right)\left(4\frac{x}{y} - 3\right) = 0$$

$$\frac{x}{y} = \frac{3}{4} \quad \text{or} \quad \frac{x}{y} = -\frac{2}{5}$$

Apply the condition $x > 0, y > 0$

Reject the negative value.

$$\boxed{x : y = 3 : 4}$$



18. a)

$$x^4 - x^2 - 3 = 0 \Rightarrow x^4 = x^2 + 3 \Rightarrow x = \sqrt[4]{x^2 + 3}$$

(b) Three iterations

$$x_{n+1} = \sqrt[4]{x_n^2 + 3}$$

- $x_0 = 1.3$

$$x_1 = \sqrt[4]{1.3^2 + 3} = \sqrt[4]{1.69 + 3} = \sqrt[4]{4.69} \approx 1.472$$

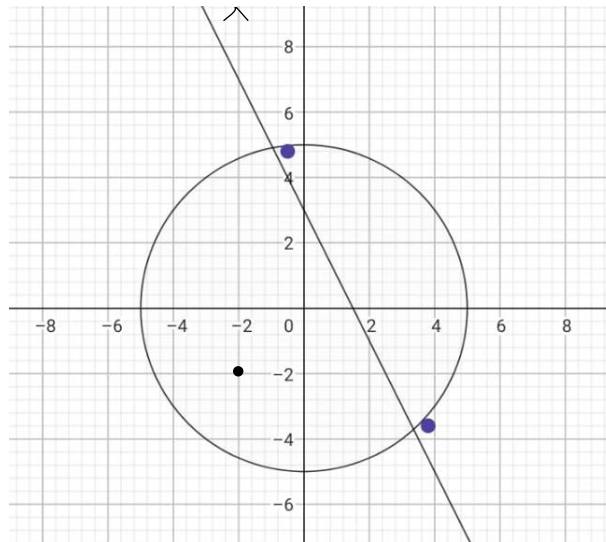
$$x_2 = \sqrt[4]{x_1^2 + 3} = \sqrt[4]{(1.4716)^2 + 3} = \sqrt[4]{2.1656 + 3} = \sqrt[4]{5.1656} \approx 1.508$$

$$x_3 = \sqrt[4]{x_2^2 + 3} = \sqrt[4]{(1.5076)^2 + 3} = \sqrt[4]{2.2728 + 3} = \sqrt[4]{5.2728} \approx 1.515$$

$$x \approx 1.515$$

19.

a)



b)

$$y = -2x + 3$$

x

x	0	1
y	3	1

x	y
-0.9	4.8
3.4	-3.7

20.

Use the product rule

$$\text{Total combinations} = (\text{laptop colours}) \times (\text{keyboard layouts}) \times (\text{storage options})$$

Let the number of keyboard layouts be x.

$$12 \times x \times 18 = 4320$$

Solve for x

$$216x = 4320$$

$$x = \frac{4320}{216} = 20$$



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21.

Since $\angle ABE = 90^\circ$, triangle ABE is right-angled at B .

$$\tan(\angle EAB) = \frac{BE}{AB}$$

$$BE = AB \tan 38^\circ = 12 \tan 38^\circ$$

$$BE \approx 12(0.7813) = 9.375 \text{ cm}$$

Find BM in the base

$DA = 12 \text{ cm}$ and $DM:MA = 3:5$ so DA is split into $3 + 5 = 8$ parts.

$$DM = \frac{3}{8} \times 12 = 4.5, MA = \frac{5}{8} \times 12 = 7.5$$

$$BM = \sqrt{(12)^2 + (7.5)^2} = \sqrt{200.25} \approx 14.151$$

Angle between EM and the base

In right triangle EBM :

$$\tan \theta = \frac{BE}{BM} = \frac{9.375}{14.151} = 0.6625$$

$$\theta = \tan^{-1}(0.6625) \approx 33.5^\circ$$

22.

Write the n th term

The sequence has first term 5 and common difference 6, so

$$u_n = 5 + (n - 1)6 = 6n - 1$$

Take two terms u_m and u_n

$$u_m = 6m - 1, u_n = 6n - 1$$

Consider the difference of their squares:

$$u_m^2 - u_n^2$$

Use difference of two squares:

$$u_m^2 - u_n^2 = (u_m - u_n)(u_m + u_n)$$

Substitute

$$u_m - u_n = (6m - 1) - (6n - 1) = 6(m - n)$$

$$u_m + u_n = (6m - 1) + (6n - 1) = 6(m + n) - 2 = 2(3(m + n) - 1)$$

$$\begin{aligned} u_m^2 - u_n^2 &= 6(m - n) \cdot 2(3(m + n) - 1) \\ &= 12(m - n)(3(m + n) - 1) \end{aligned}$$

Conclude divisibility

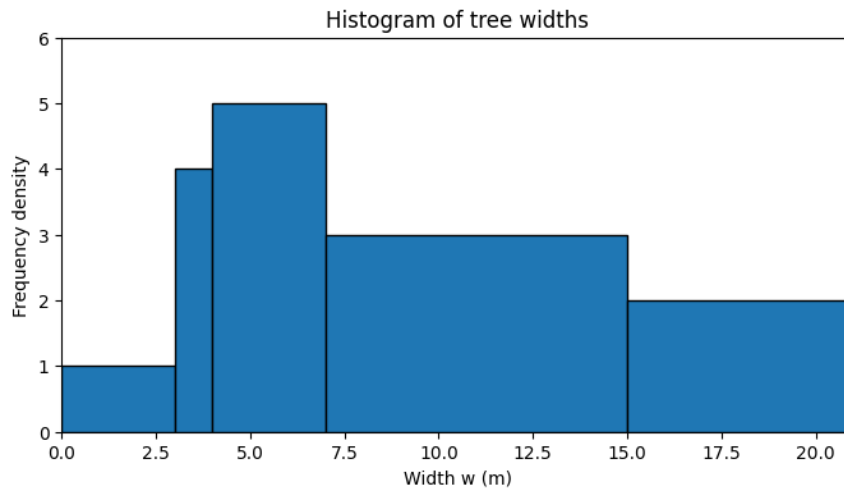
Since $(m - n)(3(m + n) - 1)$ is an integer,

$u_m^2 - u_n^2$ is always a multiple of 12.

Therefore, the difference between the squares of any two terms is divisible by 12.



23.



Calculate frequency density

$$\text{Frequency density} = \frac{\text{Frequency}}{\text{Class width}}$$

Class interval (m) Frequency density

$$0 < h \leq 3 \quad 3 \div 3 = 1$$

$$3 < h \leq 4 \quad 4 \div 1 = 4$$

$$4 < h \leq 7 \quad 15 \div 3 = 5$$

$$7 < h \leq 15 \quad 24 \div 8 = 3$$

$$15 < h \leq 21 \quad 12 \div 6 = 2$$

24.

In a trapezium with $AB \parallel DC$, the diagonals intersecting at E divide each other in the same ratio:

$$\frac{AE}{CE} = \frac{BE}{ED}$$

$$AE = 8, BE = 6, DE = 15$$

$$\frac{8}{CE} = \frac{6}{15}$$

$$\boxed{CE = 20 \text{ cm}}$$

25.

$$\cos x = \frac{\text{adjacent}}{\text{hypotenuse}} = \frac{p}{q}$$

- adjacent side = p
- hypotenuse = q

Let the opposite side be r .

Use Pythagoras' theorem

$$r^2 + p^2 = q^2$$

$$r^2 = q^2 - p^2$$

$$r = \sqrt{q^2 - p^2}$$

$$\tan x = \frac{\text{opposite}}{\text{adjacent}} = \frac{r}{p} = \frac{\sqrt{q^2 - p^2}}{p}$$

END

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GCSE

MATHEMATICS

GCSE Maths Predicted Paper 3

2026 (June): Calculator

Set 1

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Paper 3: Calculator (Set 1)
Duration: 1 hour and 30 minutes

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Grade Boundary: Grade 8: 70% and Grade 9: 82%

3.

Emma wants to buy 18 packs of floor tiles.

Here is some information about the cost of tiles from two different shops.

Tile World

- 6 packs for £78

Home Styles

- Pack of 3 costs £45
- 15% off the normal price

Emma wants to buy the 18 packs of tiles as cheaply as possible.

Should Emma buy the tiles from Tile World or from Home Styles?

You must show how you get your answer.

(3)

4.

x and y are integers such that

$$2 < x < 7, \quad 5 < y < 12$$

and

$$2x + y = 15$$

Find all possible values of x .

(4)

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8.

Triangle PQR is a right-angled triangle.

- Angle $Q = 90^\circ$
- $PR = 18$ cm
- The ratio

$$\text{size of angle } P : \text{size of angle } R = \sqrt{2} : \sqrt{3}$$

Work out the length of PQ .

(3)

9.

Shape P is reflected in the line with equation

$$x = 1$$

to give shape Q .

Shape Q is then reflected in the line with equation

$$x = 5$$

to give shape R .

Describe fully the single transformation that maps shape P directly onto shape R .

(3)

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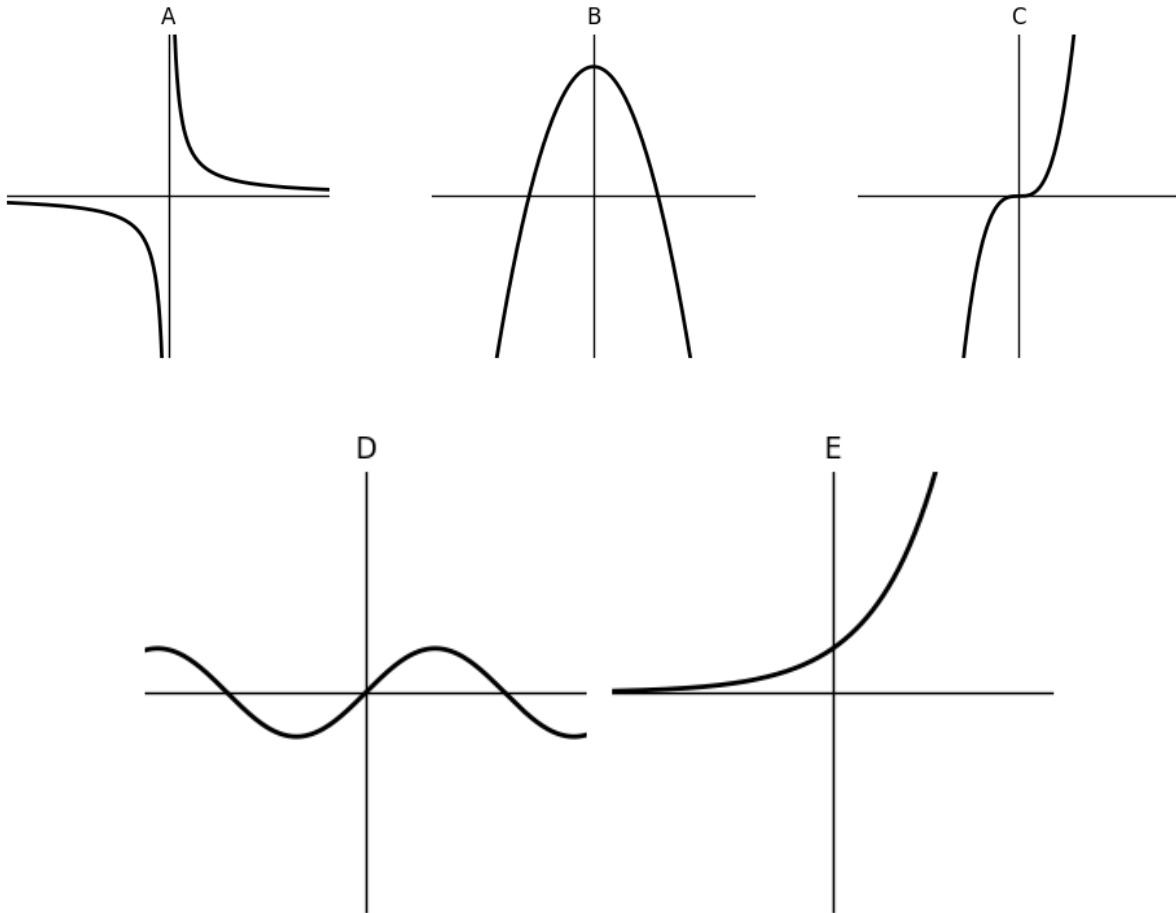
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18.



Here are five graphs, labelled A, B, C, D and E.

Each graph represents a different type of function.

The equations below are not in the same order as the graphs.

(a) $y = 2^x$

(b) $y = 4 - x^2$

(c) $y = \frac{1}{x}$

(d) $y = x^3$

Match each equation to the correct graph A, B, C, D or E.

(2)



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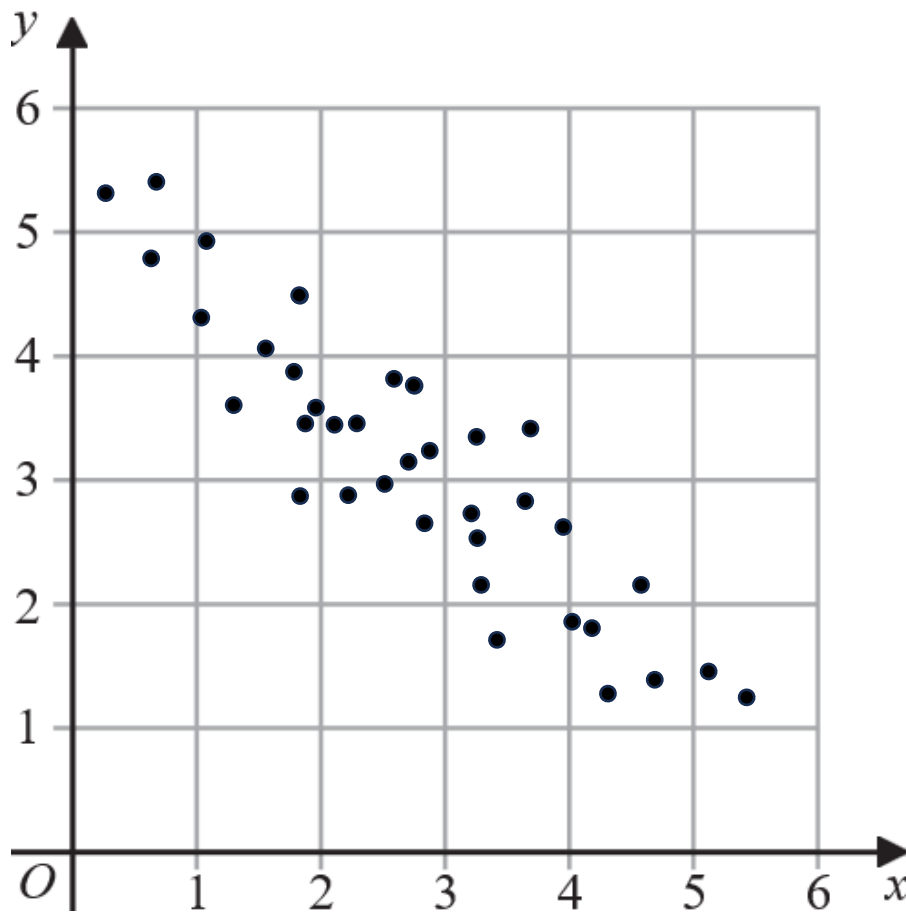
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24.

The scatter diagram the correlation between x and y values



- (a) Draw a line of best fit.
- (b) What type of correlation is shown.
- (c) Find the equation of your best fit line.

(3)



GCSE Level Maths Predicted Paper 3: 2026 (June) Set 1:

Answers

1.

Find the increase

$$416 - 320 = 96$$

Divide by the original amount

$$\frac{96}{320} = 0.3$$

Convert to a percentage

$$0.3 \times 100 = 30$$

$$\boxed{30\%}$$

2.

To compare the prices fairly, convert all prices into pounds (£).

Cycles UK

Price is already in pounds:

$$£1650$$

Vélos France (convert euros to pounds)

$$£1 = €1.30$$

$$\begin{aligned} \text{Price in pounds} &= \frac{2190}{1.30} \\ &= £1684.62 \text{ (to 2 d.p.)} \end{aligned}$$

Ride USA (convert dollars to pounds)

$$£1 = \$1.50$$

$$\begin{aligned} \text{Price in pounds} &= \frac{2550}{1.50} \\ &= £1700 \end{aligned}$$

Cycles UK sells the bicycle at the lowest price.

3.

Tile World

Each deal gives 6 packs.

Number of deals needed:

$$18 \div 6 = 3$$

Cost:

$$3 \times £78 = £234$$

Home Styles

Normal price per pack:

$$£45 \div 3 = £15$$

Apply 15% discount:

$$15\% \text{ of } £15 = 0.15 \times 15 = £2.25$$

Discounted price per pack:

$$£15 - £2.25 = £12.75$$

Cost for 18 packs:

$$18 \times \text{£}12.75 = \text{£}229.50$$

Emma should buy from Home Styles as it is cheaper.

4.

$$2 < x < 7, 5 < y < 12, 2x + y = 15$$

Make y the subject

$$y = 15 - 2x$$

Use the inequality for y

Substitute $y = 15 - 2x$ into $5 < y < 12$:

$$5 < 15 - 2x < 12$$

Solve the double inequality

$$-10 < -2x < -3$$

Divide throughout by -2 (remember to reverse the inequality signs):

$$5 > x > 1.5$$

$$1.5 < x < 5$$

Combine with the condition for x

Given:

$$2 < x < 7$$

$$2 < x < 5$$

Since x is an integer:

$$x = 3 \text{ or } x = 4$$

5.

Let the number of tokens Alex has be x .

Then:

- Bella has $3x$.
- Chris has $3x - 8$.

Total number of tokens

$$x + 3x + (3x - 8) = 69$$

$$7x - 8 = 69$$

$$7x = 77$$

$$x = 11$$

Number of tokens Chris has

$$3x - 8 = 3(11) - 8 = 33 - 8 = 25$$

Form the ratio

$$\text{Alex} : \text{Chris} = 11 : 25$$

Given the ratio is $1:n$,

$$\frac{11}{25} = \frac{1}{n} \Rightarrow n = \frac{25}{11}$$

6.

Find the lowest common multiple (LCM)

Prime factors:

- $18 = 2 \times 3^2$
- $30 = 2 \times 3 \times 5$

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- $72 = 2^3 \times 3^2$

LCM uses the highest powers:

$$\text{LCM} = 2^3 \times 3^2 \times 5 = 360$$

all three alarms sound together every 360 seconds.

Convert 2 hours to seconds

$$2 \text{ hour} = 2 \times 60 \times 60 = 7200 \text{ seconds}$$

Find how many times they sound together

$$7200 \div 360 = 20$$

7.

Left side:

$$(my^{-3})^{\frac{4}{n}} = m^{\frac{4}{n}} y^{\frac{-12}{n}}$$

$$m^{\frac{4}{n}} y^{\frac{-12}{n}} = 16y^{-2}$$

Match powers of y :

$$\frac{-12}{n} = -2 \Rightarrow -12 = -2n \Rightarrow n = 6$$

Match coefficients:

$$m^{\frac{4}{6}} = m^{\frac{2}{3}} = 16$$

Raise both sides to the power $\frac{3}{2}$:

$$m = 16^{\frac{3}{2}} = (\sqrt{16})^3 = 4^3 = 64$$

$$\boxed{n = 6, m = 64}$$

8. Triangle PQR is right-angled at Q .

Given

- $\angle Q = 90^\circ$
- $PR = 18 \text{ cm}$ (the hypotenuse)
- $\angle P : \angle R = \sqrt{2} : \sqrt{3}$

Find the angles P and R

Since the angles in a triangle add to 180° and $\angle Q = 90^\circ$:

$$\angle P + \angle R = 90^\circ$$

$$\angle P = k\sqrt{2}, \angle R = k\sqrt{3}$$

$$\angle P = \frac{90\sqrt{2}}{\sqrt{2} + \sqrt{3}}$$

Side PQ is adjacent to angle P , and PR is the hypotenuse.

$$\cos P = \frac{PQ}{PR} \Rightarrow PQ = PR \cos P$$

$$\frac{90\sqrt{2}}{\sqrt{2} + \sqrt{3}} \approx 40.8^\circ$$

$$\cos 40.8^\circ \approx 0.757$$

$$PQ = 18 \times 0.757 \approx 13.6$$

$$\boxed{PQ \approx 13.6 \text{ cm}}$$



9. A reflection in a vertical line $x = a$ followed by a reflection in a parallel vertical line $x = b$ is equivalent to a translation.

Find the distance between the two lines

$$\text{Distance} = 5 - 1 = 4$$

Because the second mirror line is to the right of the first, the overall movement is to the right.

The single transformation that maps shape P onto shape R is:

$$\boxed{\text{A translation } \begin{pmatrix} 8 \\ 0 \end{pmatrix}}$$

That is, a translation 8 units to the right.

10.

$$4x + 3y = 10$$

$$3y = 10 - 4x$$

$$y = \frac{10 - 4x}{3}$$

Substitute into the first equation

$$x^2 - 9\left(\frac{10 - 4x}{3}\right)^2 = 16$$

$$x^2 - (10 - 4x)^2 = 16$$

$$x^2 - (100 - 80x + 16x^2) = 16$$

$$15x^2 - 80x + 116 = 0$$

Using the quadratic formula:

$$x = \frac{80 \pm \sqrt{80^2 - 4(15)(116)}}{2 \cdot 15}$$

$$x = \frac{80 \pm \sqrt{6400 - 6960}}{30}$$

$$x = \frac{92}{30} = \frac{46}{15} \text{ or } x = \frac{68}{30} = \frac{34}{15}$$

Find corresponding y -values

Using $y = \frac{10 - 4x}{3}$:

When $x = \frac{46}{15}$:

$$y = \frac{10 - \frac{184}{15}}{3} = \frac{-\frac{34}{15}}{3} = -\frac{34}{45}$$

When $x = \frac{34}{15}$:

$$y = \frac{10 - \frac{136}{15}}{3} = \frac{\frac{14}{15}}{3} = \frac{14}{45}$$

$$\boxed{\left(\frac{46}{15}, -\frac{34}{45}\right) \text{ and } \left(\frac{34}{15}, \frac{14}{45}\right)}$$

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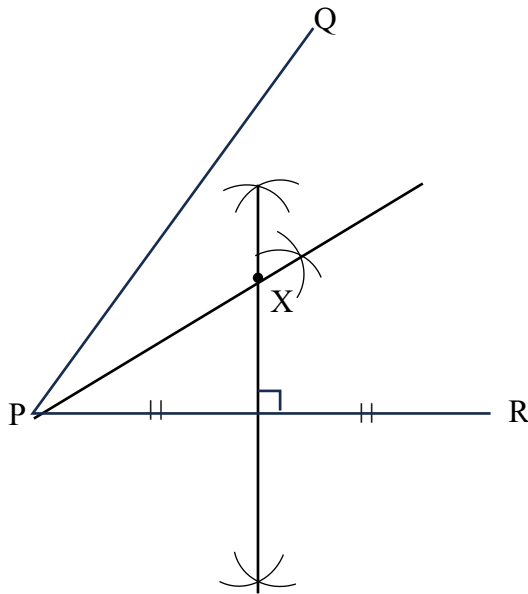
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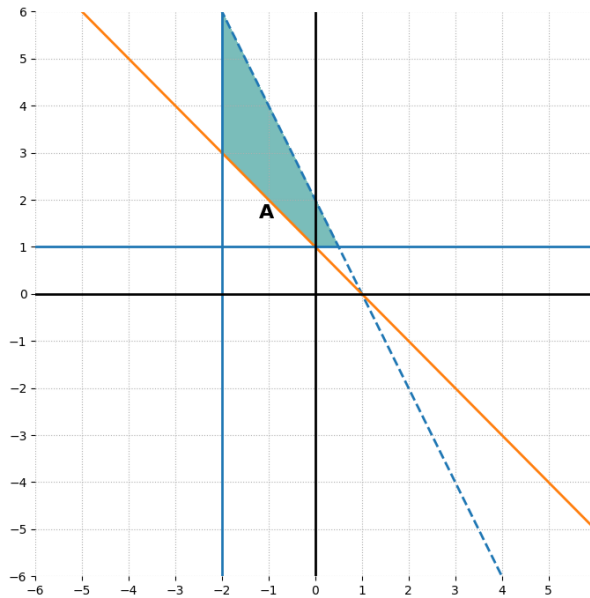
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11.
 $12 \times 11 = 132$
 12.



- 13.



14.
 Use the volume to find y

$$\text{Volume} = (3x)(4x)(y) = 12x^2y$$

Given the volume is 600:

$$12x^2y = 600$$

$$y = \frac{600}{12x^2} = \frac{50}{x^2}$$

Write the surface area formula

Surface area of a cuboid:

$$A = 2(lw + lh + wh)$$



Here:

- $l = 3x$
- $w = 4x$
- $h = y$

$$A = 2((3x)(4x) + (3x)(y) + (4x)(y))$$

$$A = 2(12x^2 + 3xy + 4xy)$$

$$A = 2(12x^2 + 7xy)$$

$$A = 24x^2 + 14xy$$

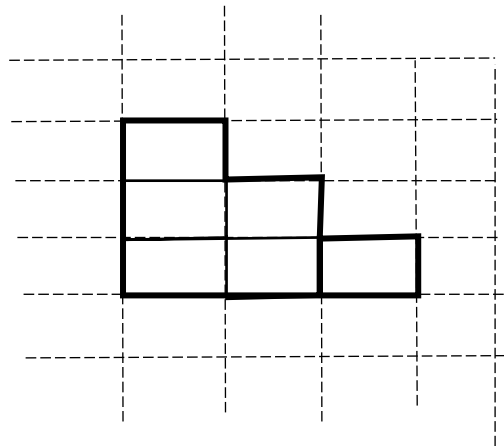
Substitute $y = \frac{50}{x^2}$

$$A = 24x^2 + 14x\left(\frac{50}{x^2}\right)$$

$$A = 24x^2 + \frac{700}{x}$$

$$A = 24x^2 + \frac{700}{x}$$

15.



16.

(a) Completed Venn diagram

- $A \cap B$ (even and prime):

$$\{2\}$$

- A only (even but not prime):

$$\{4,6,8,10\}$$

- B only (prime but not even):

$$\{3,5,7\}$$

- Outside both A and B :

$$\{1,9\}$$

(b) Probability

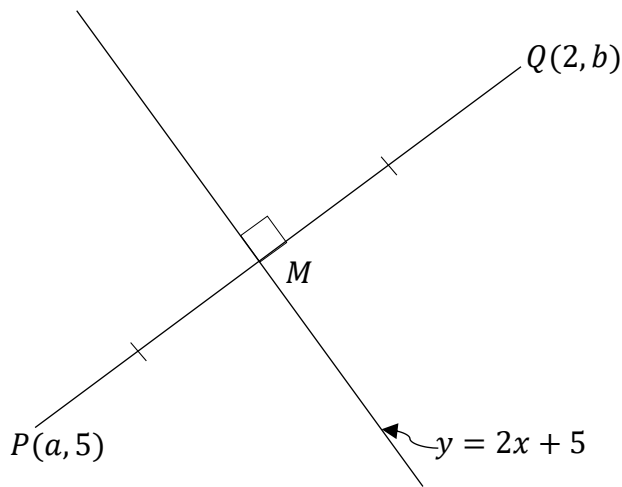
Number of elements in $U = 10$

Number of elements in $A \cap B = 1$

$$P(A \cap B) = \frac{1}{10}$$

$$\frac{1}{10}$$

17.



$$M \text{ coordinate} = \left(\frac{a+2}{2}, \frac{5+b}{2} \right)$$

$$\frac{5+b}{2} = 2 \left(\frac{a+2}{2} \right) + 5$$

$$\frac{5+b}{2} = a + 7$$

$$5 + b = 2a + 14$$

$$b - 2a = 9 \quad \text{--- (1)}$$

$$\text{Gradient of line} = 2$$

$$\text{Gradient of } PQ = -1/2$$

$$\text{Gradient Of } PQ = \frac{5-b}{a-2}$$

$$-1/2 = \frac{5-b}{a-2}$$

$$2 - a = 10 - 2b$$

$$2b - a = 8 \quad \text{--- (2)}$$

$$\text{(1)} \times 2 - \text{(2)} \Rightarrow -3a = 10$$

$$a = -10/3$$

$$\text{(1)} \Rightarrow b + 20/3 = 9$$

$$b = 7/3$$

$$\text{Midpoint} \left(\frac{-10/3+2}{2}, \frac{5+7/3}{2} \right)$$

$$\left(-2/3, 11/3 \right)$$

18.

Equation	Graph
(a) $y = 2^x$	E
(b) $y = 4 - x^2$	B
(c) $y = \frac{1}{x}$	A
(d) $y = x^3$	C

19.

Use total probability = 1

$$(n + 0.05) + 0.15 + 0.25 + 0.15 + (n + 0.10) + 0.10 = 1$$

$$2n = 0.20 \Rightarrow n = 0.10$$

Probability of landing on 1

$$P(1) = n + 0.05 = 0.10 + 0.05 = 0.15$$

Probability of landing on 1 both times

The two throws are independent:

$$P(1 \text{ both times}) = 0.15 \times 0.15 = 0.0225$$

20.

Find the radius of the circle

Since AB is tangent at A , the radius OA is perpendicular to AB .

So triangle OAB is right-angled at A .

First find OB :

$$OB = \sqrt{18^2 + 4^2} = \sqrt{324 + 16} = \sqrt{340}$$

In right triangle OAB , with $\angle OBA = 30^\circ$,

$$\sin 30^\circ = \frac{OA}{OB}$$

$$OA = OB \sin 30^\circ = \sqrt{340} \cdot \frac{1}{2} = \frac{\sqrt{340}}{2}$$

So the radius is $r = OA = \frac{\sqrt{340}}{2}$. Hence

$$r^2 = \left(\frac{\sqrt{340}}{2}\right)^2 = \frac{340}{4} = 85$$

Use the circle equation $x^2 + y^2 = r^2$

Point $P(3p - 2, 2p + 1)$ lies on the circle, so:

$$(3p - 2)^2 + (2p + 1)^2 = 85$$

Expand:

$$(9p^2 - 12p + 4) + (4p^2 + 4p + 1) = 85$$

$$13p^2 - 8p + 5 = 85$$

$$13p^2 - 8p - 80 = 0$$

Solve the quadratic

$$13p^2 - 8p - 80 = 0$$

$$p = \frac{8 \pm \sqrt{(-8)^2 - 4(13)(-80)}}{2 \cdot 13} = \frac{8 \pm \sqrt{64 + 4160}}{26} = \frac{8 \pm \sqrt{4224}}{26}$$

Since p must give a valid point on the diagram, take the positive value:

$$\boxed{p = 2.8}$$

21.

Write $\tan a$ and $\tan b$

For a right-angled triangle,

$$\tan(\text{angle}) = \frac{\text{opposite}}{\text{adjacent}}$$

$$\tan a = \frac{x + 2}{5x - 3}$$

$$\tan b = \frac{4x - 1}{10x + 7}$$

Use the given condition

$$\tan a = 2 \tan b$$

$$\frac{x+2}{5x-3} = 2 \left(\frac{4x-1}{10x+7} \right)$$

$$(x+2)(10x+7) = 10x^2 + 27x + 14$$

Set equal:

$$10x^2 + 27x + 14 = 40x^2 - 34x + 6$$

Rearrange:

$$0 = 30x^2 - 61x - 8$$

Using the quadratic formula:

$$x = \frac{61 \pm \sqrt{61^2 - 4(30)(-8)}}{2(30)}$$

$$x = \frac{61 \pm \sqrt{3721 + 960}}{60} = \frac{61 \pm \sqrt{4681}}{60}$$

Since side lengths must be positive:

$$5x - 3 > 0 \Rightarrow x > 0.6$$

$$x = \frac{61 + \sqrt{4681}}{60} = 2.16$$

22.

(a) Finding the value of y

For a geometric sequence, the common ratio is the same between consecutive terms.

$$\frac{3}{\sqrt{y}+1} = \frac{\sqrt{y}-1}{3}$$

Cross-multiply:

$$9 = (\sqrt{y}+1)(\sqrt{y}-1)$$

Use the identity $(a+b)(a-b) = a^2 - b^2$:

$$9 = y - 1$$

$$y = 10$$

23.

Find BD using cosine rule in $\triangle ABD$

$$BD^2 = AB^2 + AD^2 - 2(AB)(AD)\cos 68^\circ$$

$$BD^2 = 10.6^2 + 13.2^2 - 2(10.6)(13.2)\cos 68^\circ$$

$$BD \approx 13.48 \text{ cm}$$

Use sine rule in $\triangle BCD$

Now use sine rule:

$$\frac{BC}{\sin 42^\circ} = \frac{BD}{\sin 57^\circ}$$

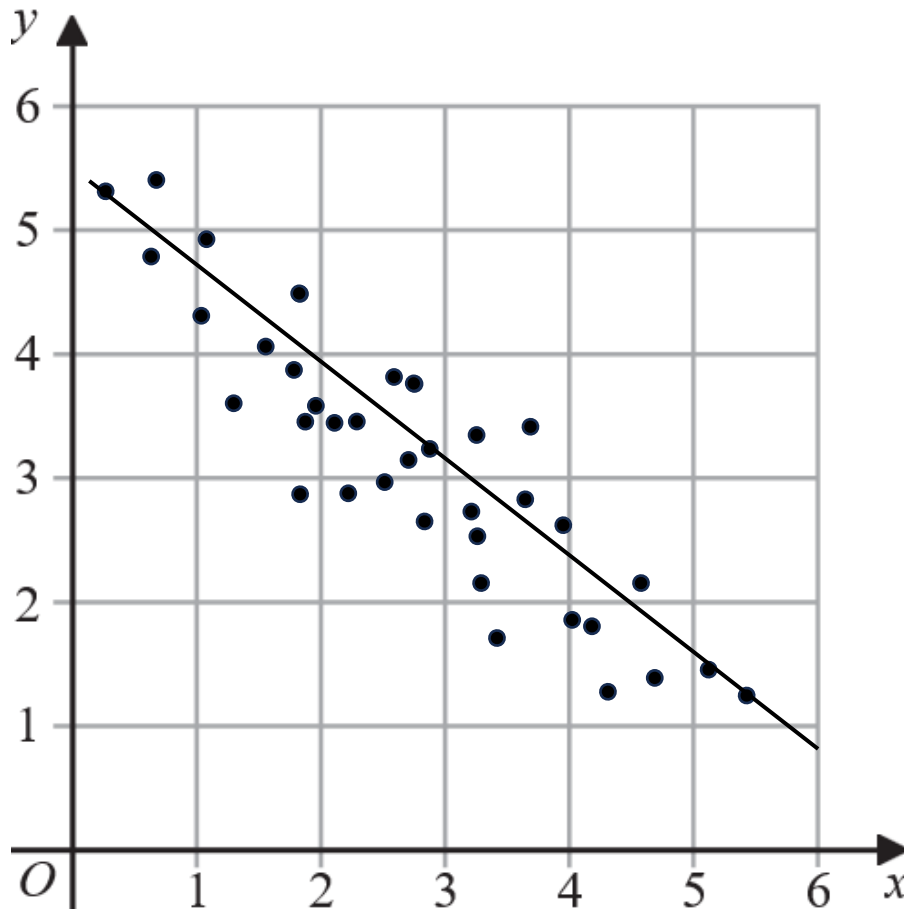
$$BC = BD \cdot \frac{\sin 42^\circ}{\sin 57^\circ} = 13.48 \cdot \frac{\sin 42^\circ}{\sin 57^\circ}$$

$$BC \approx 10.7567 \approx 10.8 \text{ cm}$$

$$BC = 10.8 \text{ cm (3 s.f.)}$$

24.

(a)



b) Type of correlation

The points clearly slope downwards as x increases, so this shows negative correlation (fairly strong).

Negative correlation

(c) Equation of a suitable best-fit line

Using two reasonable points on the trend, e.g. (1,4.8) and (5,1.6):

Gradient:

$$m = \frac{1.6 - 4.8}{5 - 1} = \frac{-3.2}{4} = -0.8$$

Use $y = mx + c$ with (1,4.8):

$$4.8 = -0.8(1) + c \Rightarrow c = 5.6$$

$$y = -0.8x + 5.6$$

25.

Find r (midline)

Maximum value of $y = 4$

Minimum value of $y = -2$

The midline is:

$$r = \frac{4 + (-2)}{2} = \frac{2}{2} = 1$$

$$\boxed{r = 1}$$

Find p (amplitude)

Amplitude is:

$$p = \frac{4 - (-2)}{2} = \frac{6}{2} = 3$$

$$\boxed{p = 3}$$

Find q (horizontal shift)

A sine graph reaches its maximum when:

$$x + q = 90^\circ$$

The graph reaches its maximum at $x = 60^\circ$

$$60 + q = 90$$

$$q = 30$$

$$\boxed{q = 30}$$

$$\boxed{p = 3, q = 30, r = 1}$$

END

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